

# Computational study of the intramolecular proton transfer reactions of 3-hydroxytropolone (2,7-dihydroxycyclohepta-2,4,6-trien-1-one) and its dimers

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Received: 31 August 2009 / Accepted: 2 February 2010 / Published online: 16 March 2010  
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**Abstract** The proton transfer reaction and dimerization processes of 3-hydroxytropolone (3-OHTRN) have been investigated using density functional theory (DFT) at the B3LYP/6-31+G\*\* level. The influence of the solvent on the proton transfer reaction of 3-OHTRN was examined using the self-consistent isodensity polarized continuum model (SCI-PCM) with different dielectric constants ( $\epsilon=4.9$ ,  $\text{CHCl}_3$ ;  $\epsilon=32.63$ ,  $\text{CH}_3\text{OH}$ ;  $\epsilon=78.39$ ,  $\text{H}_2\text{O}$ ). The intramolecular proton transfer reaction occurs more readily in the gas phase than in solution. Results also show that the stability of 3-OHTRN dimers in the gas phase is directly affected by the hydrogen bond length in the dimer structure.

**Keywords** Hydrogen bonding · Tropolone derivative · Proton transfer reaction · Dimer

## Introduction

Lots of theoretical and experimental studies have been carried out to enhance knowledge of the mechanisms of proton transfer, tautomeric equilibrium and relevant properties, since *intra*- and *inter*molecular proton transfer play key roles in many chemical and biological processes [1–15].

Tropolone and its derivatives have been explored experimentally [16–25] and theoretically [26–32] as model compounds for intramolecular proton transfer. Tropolone (TRN) is a nonbenzoid seven-membered ring

( $\text{C}_7\text{O}_3\text{H}_6$ ). It can act as a hydrogen bond donor or a hydrogen bond acceptor because of its acidic OH proton and its basic C=O groups. Thus, it can form both intramolecular hydrogen bonds and intermolecular hydrogen bonds. The X-ray structure of tropolone shows that the molecules are arranged as centrosymmetric hydrogen-bonded dimers [33, 34]. X-ray diffraction studies show that the hydrogen-bonded dimer is the dominant species in the tropolone crystal, comprising more than 98% of the molecules in the crystal at room temperature (Olender Z, private communication).

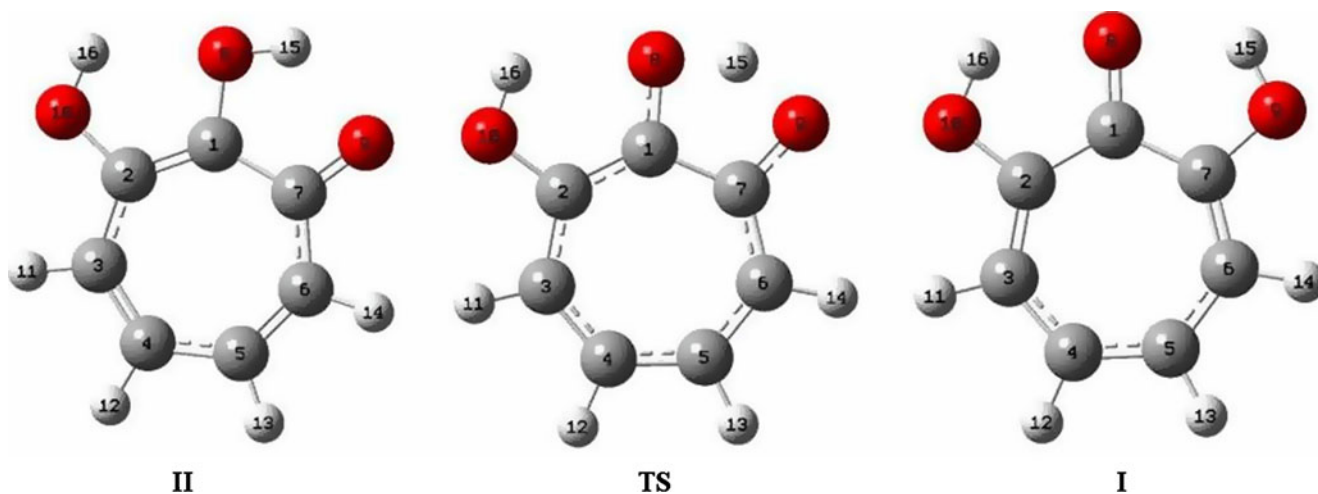
3-OHTRN (3-hydroxytropolone, a derivative of TRN), exhibits two tautomers, 2,7-dihydroxycyclohepta-2,4,6-trien-1-one (I) and 2,3-dihydroxycyclohepta-2,4,6-trien-1-one (II) [35]. In this paper, we report on our investigation of the proton transfer reaction between the I and II tautomers (see Fig. 1) of 3-OHTRN. In this work, we carried out calculations using Becke's three-parameter hybrid functional (B3LYP) methods [36, 37] for 3-OHTRN in chloroform, in methanol and in water in order to evaluate the effect of the solvent on tautomerization. Additionally, computations on 3-OHTRN dimers with two different structures were performed in the gas phase at the same calculation level. Based on a search of the literature, this is the first computational study of the proton transfer reaction between two tautomers of 3-OHTRN and the proton transfer reaction between their dimers. Therefore, we hope that our study provides an enhanced interpretation of tautomers of 3-OHTRN and their dimer structures.

## Methods

The stationary structures (I and II) in the proton transfer reaction of 3-OHTRN were optimized using the most

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**Fig. 1** Optimized molecular structures of I, II and the transition state (TS) (obtained using GaussView 3.0 [42])

popular B3LYP [36, 38] method by applying the 6–31+G\*\* basis set with polarization functions on all atoms and diffuse functions on heavy atoms in the gas phase. The vibrational frequencies were obtained at the same level to characterize the local minimum and the transition states (corresponding to a single negative eigenvalue of the Hessian). The basis set superposition error (BSSE) associated with the hydrogen bond energy was computed via the counterpoise method using the individual bases as fragments [39]. In order to take into account the bulk of the solvent, we performed an SCRF calculation using a cavity determined self-consistently from the self-consistent isodensity polarized continuum model (SCI-PCM) [40] with different dielectric constants ( $\epsilon=4.9$ ,  $\text{CHCl}_3$ ;  $\epsilon=32.63$ ,  $\text{CH}_3\text{OH}$ ;  $\epsilon=78.39$ ,  $\text{H}_2\text{O}$ ). All the calculations were performed with the Gaussian 03W computational package [41].

## Discussion

The B3LYP/6–31+G\*\* optimized geometries for I, II and TS (the transition state) are shown in Fig. 1, and selected structural parameters are listed in Table 1.

The proton transfer reaction  $\text{II} \rightarrow \text{TS} \rightarrow \text{I}$  was considered. The transfer of a hydrogen atom from the  $\text{O}_8$  to the  $\text{O}_9$  atom is accompanied by a rearrangement of the seven-membered ring, and substantial changes are observed in the carbon–oxygen and oxygen–hydrogen bonds. The distance between  $\text{O}_9$  and  $\text{H}_{15}$  decreases upon the proton transfer  $\text{II} \rightarrow \text{TS} \rightarrow \text{I}$ . The  $\text{O}_8\text{--H}_{15}$  and  $\text{O}_9\text{--H}_{15}$  distances for TS are 1.194 Å and 1.282 Å in the gas phase. It can be concluded that the  $\text{O}_8\text{--H}_{15}$  bond is broken and an  $\text{O}_9\text{--H}_{15}$  bond is formed during the proton transfer process in 3-OHTRN. In the proton transfer  $\text{II} \rightarrow \text{TS} \rightarrow \text{I}$ , the  $\text{C}_1\text{--C}_7$  and  $\text{C}_1\text{--C}_8$  distances decrease, the  $\text{C}_7\text{--C}_9$  and  $\text{C}_1\text{--C}_2$

distances increase, while the angle  $\text{O}_8\text{C}_1\text{C}_7$  first decreases and then increases in all phases. The  $\text{C}_1\text{O}_8\text{H}_{15}$  angle decreases on  $\text{II} \rightarrow \text{I}$  transfer, while the  $\text{C}_7\text{O}_9\text{H}_{15}$  angle increases in all phases.

Let's see how the calculated tautomerization energy for 3-OHTRN changes. The tautomerization energy, as shown in Fig. 2, was calculated as the energy differences between the tautomers and the transition states. The energy differences between the two tautomers (I and II) were calculated to be  $-5.52$ ,  $-4.73$ ,  $-4.42$ ,  $-4.38$  kcal mol $^{-1}$  in the gas phase, in chloroform, in methanol, and in water, respectively. That is, tautomer I is more stable than tautomer II in the gas phase and in solution.

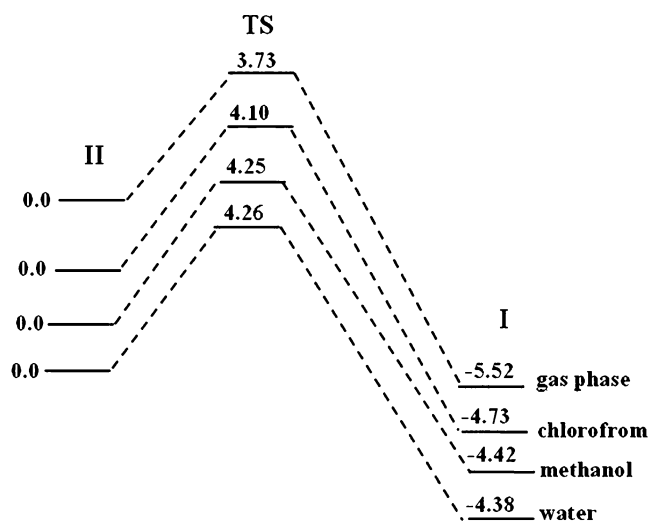
The relative energies of the TS with respect to tautomer II were calculated to be 3.73, 4.10, 4.25 and 4.26 kcal mol $^{-1}$  in the gas phase, in chloroform, in methanol, and in water, respectively. The barrier height decreases on going from the water phase to the gas phase. As a result, the intramolecular proton transfer reaction between structures I and II occurs more easily in the gas phase than in solution. Similar barrier heights were observed for all of the solutions. However, we can conclude that the stronger the dipole moment of the solvent, the higher the barrier to the proton transfer process.

From the viewpoint of valence theory, the interaction between the lone pair of the acceptor O atom and  $\text{O}\text{--H}$   $\sigma^*$  orbitals is mainly responsible for the proton transfer. Therefore, the  $\text{O}\dots\text{H}\text{--O}$  angle and the  $\text{O}\dots\text{H}$  distance (in tautomer II) may play important roles in the proton transfer reactions. In most cases, hydrogen bonds with linear  $\text{O}\dots\text{H}\text{--O}$  structures and short hydrogen bond distances are considered to be strong. In tautomer II, the  $\text{O}_8\text{--H}_{15}\dots\text{O}_9$  angles are  $122.80^\circ$ ,  $121.98^\circ$ ,  $121.69^\circ$  and  $121.61^\circ$  in the gas phase, in chloroform, in methanol, and in water, respectively. Additionally, the  $\text{O}_8\text{--H}_{15}\dots\text{O}_9$  hydrogen bond distances of tautomer II are 1.820 Å, 1.842 Å, 1.851 Å and

**Table 1** Selected bond lengths, bond angles and dihedrals as derived from B3LYP (6-31+G\*\*) geometric optimization of 3-OHTRN in the gas phase and in solution

Parameters <sup>a</sup>	Gas phase						Chloroform ( $\epsilon=4.9$ )			Methanol ( $\epsilon=32.63$ )			Water ( $\epsilon=78.39$ )		
	I	TS	II	I	TS	II	I	TS	II	I	TS	II	I	TS	II
	<b>Bond length</b>														
C <sub>1</sub> C <sub>7</sub>	1.449	1.459	1.462	1.447	1.456	1.459	1.446	1.455	1.457	1.446	1.455	1.457	1.446	1.455	1.457
C <sub>1</sub> C <sub>2</sub>	1.449	1.400	1.384	1.447	1.400	1.386	1.446	1.401	1.387	1.446	1.401	1.387	1.446	1.401	1.387
C <sub>7</sub> O <sub>9</sub>	1.347	1.292	1.259	1.350	1.299	1.263	1.351	1.302	1.266	1.351	1.302	1.266	1.351	1.302	1.266
C <sub>1</sub> O <sub>8</sub>	1.266	1.310	1.350	1.270	1.313	1.352	1.270	1.314	1.352	1.271	1.314	1.352	1.271	1.314	1.352
C <sub>2</sub> O <sub>10</sub>	1.347	1.359	1.363	1.350	1.359	1.362	1.351	1.358	1.362	1.351	1.358	1.362	1.351	1.358	1.362
O <sub>10</sub> H <sub>16</sub>	0.983	0.974	0.971	0.983	0.973	0.972	0.983	0.973	0.972	0.982	0.973	0.972	0.982	0.973	0.972
O <sub>9</sub> H <sub>15</sub>	0.983	1.282	1.820	0.983	1.273	1.842	0.983	1.269	1.851	0.982	1.269	1.852	0.982	1.269	1.852
O <sub>8</sub> ...H <sub>15</sub>	1.919	1.194	0.994	1.931	1.198	0.991	1.936	1.200	0.990	1.937	1.200	0.990	1.937	1.200	0.990
O <sub>8</sub> ...H <sub>16</sub>	1.919	2.126	2.074	1.931	2.151	2.086	1.936	2.162	2.090	1.937	2.162	2.093	1.937	2.162	2.093
<b>Bond angle</b>															
O <sub>8</sub> C <sub>1</sub> C <sub>7</sub>	117.63	109.35	112.37	117.72	109.44	112.73	117.76	109.47	112.89	117.76	109.47	112.89	117.76	109.47	112.89
O <sub>8</sub> C <sub>1</sub> C <sub>2</sub>	117.63	120.65	116.23	117.72	120.84	116.07	117.76	120.92	115.96	117.76	120.90	116.00	117.76	120.90	116.00
C <sub>1</sub> C <sub>2</sub> O <sub>10</sub>	112.66	116.68	117.91	112.78	116.90	117.99	112.81	117.00	118.01	112.84	117.00	118.05	112.84	117.00	118.05
C <sub>1</sub> C <sub>7</sub> O <sub>9</sub>	112.66	108.83	114.66	112.78	108.69	114.77	112.81	108.64	114.85	112.84	108.63	114.82	112.84	108.63	114.82
C <sub>7</sub> O <sub>9</sub> H <sub>15</sub>	105.14	–	–	105.45	91.71	87.06	105.64	–	–	105.64	–	–	105.64	–	–
C <sub>2</sub> O <sub>10</sub> H <sub>16</sub>	105.14	107.76	108.74	105.45	108.57	109.53	105.64	108.92	109.83	105.64	108.95	109.92	105.64	108.95	109.92
C <sub>1</sub> O <sub>8</sub> H <sub>15</sub>	–	–	102.90	84.45	91.90	103.46	–	–	103.64	–	–	–	–	–	103.72
O <sub>8</sub> H <sub>15</sub> O <sub>9</sub>	120.05	137.83	122.80	119.60	138.26	121.98	119.34	138.43	121.69	119.33	138.45	121.61	119.33	138.45	121.61
<b>Dihedrals</b>															
O <sub>8</sub> C <sub>1</sub> C <sub>2</sub> C <sub>3</sub>	179.97	–180.00	180.00	–180.00	–180.00	180.00	180.00	–180.00	–179.97	–180.00	–180.00	–0.003	–180.00	–180.00	–0.003
O <sub>8</sub> C <sub>1</sub> C <sub>7</sub> O <sub>9</sub>	0.035	–0.005	–0.006	–0.0012	–0.002	0.0160	0.010	–0.003	0.031	–0.026	–0.003	0.027	–0.026	–0.003	0.027
C <sub>1</sub> C <sub>2</sub> O <sub>10</sub> H <sub>16</sub>	–0.006	0.000	0.002	0.0004	0.0004	–0.0020	–0.001	0.00	0.045	0.004	0.000	–0.003	0.004	0.000	–0.003
C <sub>1</sub> C <sub>7</sub> O <sub>9</sub> H <sub>15</sub>	0.006	–	–	–0.0004	0.0010	–0.0190	0.001	–	–	0.004	–	–	0.004	–	–

<sup>a</sup> Distances in Å; angles in degrees. For numbering of atoms, see Fig. 1



**Fig. 2** Energy diagram of the proton transfer process in various solvents (via SCI-PCM) and in the gas phase

1.852 Å in the gas phase, in chloroform, in methanol, and in water, respectively. The existence of a strong  $O_8-H_{15}\dots O_9$  hydrogen bond in tautomer II shows that the barrier to the intramolecular proton transfer may have been low in the gas phase. Another reason for this result is that the distance of  $O_8$  from  $H_{15}$  in the TS structure is shortest in the gas phase.

Let's now examine the calculated relative free energies ( $\Delta G$ ) and activation free energy barriers ( $\Delta G^\ddagger$ ) for the proton transfer reaction of 3-OHTRN in the gas phase and in solutions. As seen in Table 2, the free energy for the proton transfer reaction of 3-OHTRN is lowest in the gas phase. The activation free energy barrier height decreases on going from the water phase to the gas phase. As a result, according to  $\Delta G$  and  $\Delta G^\ddagger$ , this reaction is thermodynamically and kinetically easier in the gas phase than it is in solution.

When we look at the calculated  $\Delta E_s$  and  $\Delta G_s$  values in Table 3, we see that tautomer II is the more stable of the tautomeric structures, presumably due to solvent effects. In addition, solvent effects mean that the TS structure in solution is more stable than it is in the gas phase. Consequently, the energy barrier to proton transfer reaction increases in solution.

**Table 2** Calculated free energies and activation free energy barriers (in kcal mol<sup>-1</sup>) for the proton transfer reaction of 3-OH-TRN

	$\Delta G$	$\Delta G^\ddagger$
Gas phase	-5.15	1.74
Chloroform	-4.42	2.11
Methanol	-4.13	2.25
Water	-4.08	2.28

## Dimers

The structural parameters of the dimer structures (I-D and II-D) calculated at the B3LYP/6-31+G\*\* level are shown in Fig. 3.

The optimized geometrical parameters indicate that the two tautomers (I and II) are fully planar, in agreement with experimental values [43]. The planarity of these structures is attributed to the strong intramolecular hydrogen bonding and the structure of the tropolone ring.

A study of the crystal structure of 3-OHTRN has shown that the  $O_9-H_{15}\dots O_8$  hydrogen bond length is 1.930 Å, the  $O-H\dots O$  angle is 122.4°, and the  $C_1-O_8$  and  $C_7-O_9$  bond lengths are 1.263 Å and 1.346 Å [43]. The calculated  $O_9-H_{15}\dots O_8$  hydrogen bond length and the  $O_9-H_{15}\dots O_8$  angle are 1.919 Å and 120.05°, respectively, for tautomer I in the gas phase. The calculated  $C_1-O_8$  and  $C_7-O_9$  bond lengths are 1.263 Å and 1.347 Å, respectively, in the gas phase (see Table 1). These calculated values are in good agreement with the experimental data.

Two tautomer I structures are bonded to each other with two intermolecular hydrogen bonds in the I-D structure [43], while two tautomer II structures are bonded to each other with two intermolecular hydrogen bonds in the II-D structure. These two hydrogen bonds in the dimer structures are equivalent to each other (see Fig. 3).

Comparing the monomer and dimer structures in the gas phase, it has been noted that the intermolecular hydrogen bonds affect the molecular structure of the monomer. As seen in Table 1 and Fig. 3, the bond angles and lengths of the hydrogen donor (O-H) and hydrogen acceptor (C=O) groups of the I-D and II-D structures differ from those of their monomers. For example; the  $C_2O_{10}H_{16}$  and  $O_8C_1C_2$  angles are increased by 7.38° and 1.90° in I-D, respectively. The  $C_1O_8H_{15}$  and  $C_1C_7O_9$  angles are increased by 11.67° and 2.87° in II-D, respectively. Another important point is the changes in the  $C_1O_8$  ( $C_7O_9$ ) and  $O_{10}H_{16}$  ( $O_8H_{15}$ ) bond lengths on going from the monomers to the dimeric structures. The results obtained for the gas phase show that the  $C_1O_8$  and  $O_{10}H_{16}$  bond lengths are 0.003 Å longer in I-D. The  $C_7O_9$  and  $O_8H_{15}$  bond lengths are 0.001 Å shorter in II-D. Additionally, there are changes in the intramolecular hydrogen bonds on going from the monomers to the dimeric structures. The  $O_8\dots H_{16}$  hydrogen bond lengthens by 0.252 Å, while the  $O_8\dots H_{15}$  hydrogen bond shortens by 0.046 Å in I-D. The  $O_9\dots H_{15}$  hydrogen bond lengthens by 0.393 Å, while the  $O_8\dots H_{16}$  hydrogen bond shortens by 0.113 Å in II-D.

The values of the calculated uncorrected interaction energies,  $\Delta E$ , and the corrected interaction energies,  $\Delta E_c$ , are given in Table 4. The interaction energies are corrected for basis set superposition error (BSSE) at the B3LYP level

**Table 3** Dipole moments ( $\mu$ , in debyes), solvation energies  $\Delta E_s = E_{\text{gas}} - E_{\text{solv}}$ , and solvation Gibbs free energies  $\Delta G_s = G_{\text{gas}} - G_{\text{solv}}$  (kcal mol<sup>-1</sup>) of the tautomeric forms in the gas phase and in solution

	Gas phase	Chloroform		Methanol			Water			
	$\mu$	$\Delta E_s$	$\Delta G_s$	$\mu$	$\Delta E_s$	$\Delta G_s$	$\mu$	$\Delta E_s$	$\Delta G_s$	$\mu$
I	3.12	-3.34	-3.62	3.94	-4.56	-4.97	4.23	-4.71	-5.13	4.26
II	3.14	-4.13	-4.36	3.96	-5.67	-6.00	4.27	-5.84	-6.20	4.30
TS	3.54	-3.76	-3.99	4.51	-5.15	-5.67	4.88	-5.32	-5.67	4.92

using an approximation to the Boys–Bernardi counterpoise method [39], as described below.

The hydrogen-bonding interaction energy,  $\Delta E$ , of the dimer (for example I-D) is defined as

$$\Delta E = E_{I...I} - E_I - E_I, \quad (1)$$

where  $E_{I...I}$  refers to the energy of the I-D, and  $E_I$  is the energy of tautomer I. When the BSSE is taken into account, the BSSE-corrected interaction energy,  $\Delta E_c$ , is then calculated as

$$\Delta E_c = E_{I...I} - E_{I(I...I)} - E_{I(I...I)} \quad (2)$$

where  $E_{I(I...I)}$  is the energy of monomer I obtained with the extra ghost Gaussian functions placed at the positions of monomer I in the dimer.

As seen from these calculated interaction energies, II-D is more stable than I-D. When we look at the calculated  $\Delta G$  values in Table 4, II-D is more stable than I-D by 1.57 kcal mol<sup>-1</sup>. It is interesting that the intermolecular hydrogen bond lengths in II-D are shorter than those in the

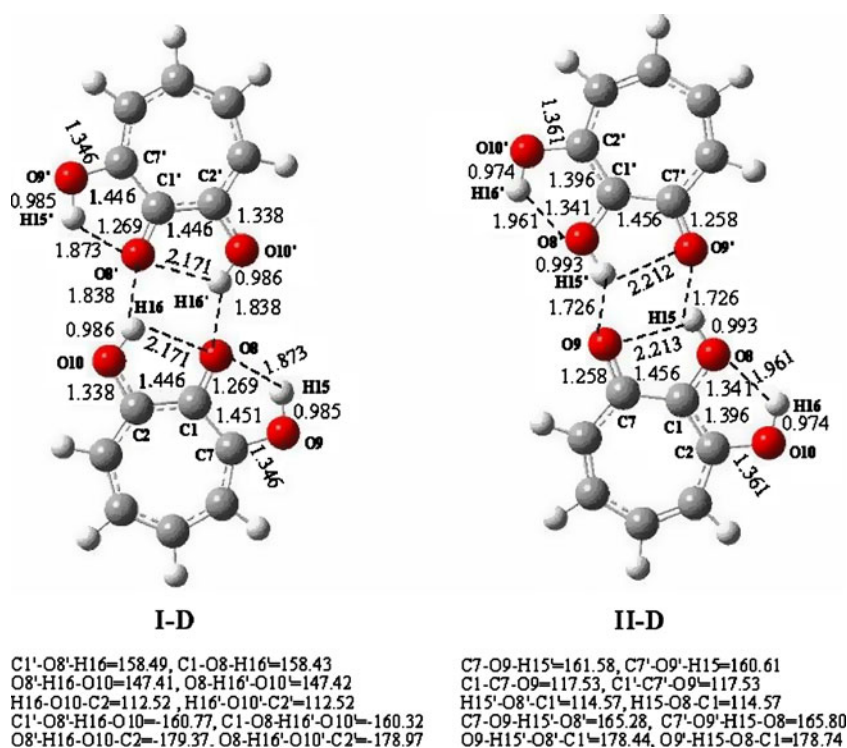
I-D structure. Thus, the stabilities of the dimer structures under investigation can explain the intermolecular hydrogen bonds formed in the dimers.

## Conclusions

The major conclusions to be gleaned from this work are as follows:

1. Tautomer I is more stable than tautomer II in the gas phase and in solution.
2. The barrier height for the proton transfer reaction of 3-OHTRN decreases upon shifting from the water phase to the gas phase. As a result, the intramolecular proton transfer reaction between structures I and II is thermodynamically and kinetically easier in the gas phase than in solution.
3. The geometrical parameters of the two monomer molecules in the I-D and II-D structures are nearly the same.

**Fig. 3** Optimized structures of the I-D and II-D structures. Bond lengths are shown in Å and angles in degrees (obtained using GaussView 3.0 [42])



**Table 4** Calculated free energies  $\Delta G$ , interaction energies  $\Delta E$ , BSSEs, and corrected interaction energies  $\Delta E_c$  for the dimerization of tautomers of 3-OHTRN in the gas phase

Structures	$\Delta E$	BSSE	$\Delta E_c$	$\Delta G$
I-D	-6.84	0.91	-5.93	5.28
II-D	-8.45	0.95	-7.50	3.71

- II-D is more favorable than I-D. That is, the intermolecular hydrogen bonds in the II-D structure are stronger than those in the I-D structure.
- The results show that the stabilities of the dimer structures are directly affected by the hydrogen bond lengths in the dimer structures.
- At this time, there are no published data from computational investigations of the intramolecular proton transfer reactions of 3-hydroxytropolone and its dimers, so our calculations provide a useful interpretation of literature data.

**Acknowledgments** The authors acknowledge the CUBAP (The Scientific Research Projects Council of Cumhuriyet University) for the providing the Gaussian 03W and GaussView 3.0 program packages.

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